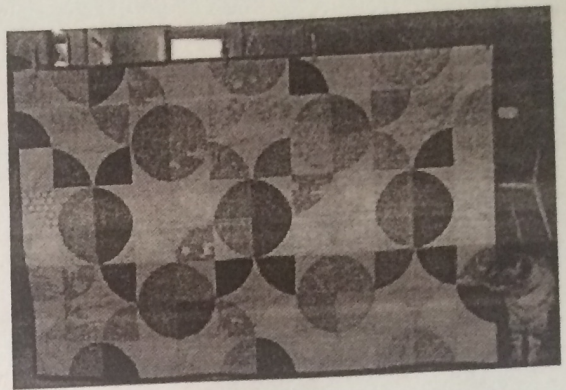


2.5 BE THERE OR BE SQUARE

A Practice Understanding Task



Quilts and Quadratic Graphs

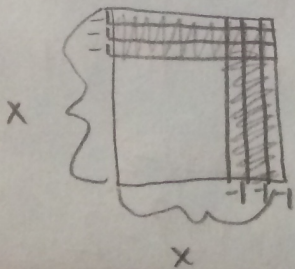
Optima's niece, Jenny works in the shop, taking orders and drawing quilt diagrams. When the shop isn't too busy, Jenny pulls out her math homework and works on it. One day, she is working on graphing parabolas and notices that the equations she is working with looks a lot like an order for a quilt block. For instance, Jenny is supposed to graph the equation: $y = (x - 3)^2 + 4$. She thinks, "That's funny. This would be an order where the length of the standard square is reduced by 3 and then we add a little piece of fabric that has an area of 4. We don't usually get orders like that, but it still makes sense. I better get back to thinking about parabolas. Hmmm..."

1. Fully describe the parabola that Jenny has been assigned to graph.

The parabola would have been shifted to the right 3 and moved up 4.
Vertex: (3, 4)

2. Jenny returns to her homework, which is about graphing quadratic functions. Much to her dismay, she finds that she has been given: $y = x^2 - 6x + 9$. "Oh dear", thinks Jenny. "I can't tell where the vertex is or identify any of the transformations of the parabola in this form. Now what am I supposed to do?"

"Wait a minute—is this the area of a perfect square?" Use your work from *Building the Perfect Square* to answer Jenny's question and justify your answer.

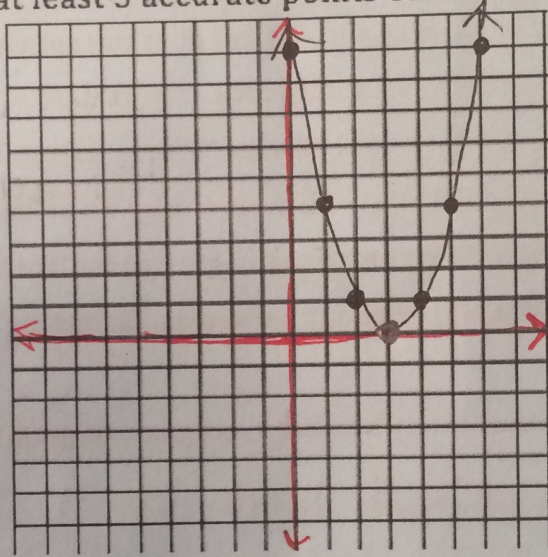


Yes, this would be a perfect square because all pieces of the equations were used, we didn't have to adjust at all.

3. Jenny says, "I think I've figured out how to change the form of my quadratic equation so that I can graph the parabola. I'll check to see if I can make my equation a perfect square." Jenny's equation is: $y = x^2 - 6x + 9$.

See if you can change the form of the equation, find the vertex, and graph the parabola.

- a. $y = x^2 - 6x + 9$ New form of the equation: $y = (x-3)^2$
- b. Vertex of the parabola: $(3, 0)$
opposite of what's in parentheses.
- c. Graph (with at least 3 accurate points on each side of the line of symmetry):



$y = (x-3)^2$
inside part came from side length of square

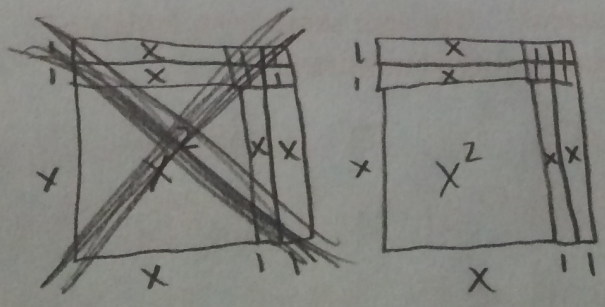
Vertex $(3, 0)$ ← starting point

over 1, up 1
 over 2, up 4
 over 3, up 9

4. The next quadratic to graph on Jenny's homework is $y = x^2 + 4x + 2$. Does this expression fit the pattern for a perfect square? Why or why not?

No, the equation needs to be $x^2 + 4x + 4$ for it to be a perfect square.

- a. Use an area model to figure out how to complete the square so that the equation can be written in vertex form, $y = a(x-h)^2 + k$.



original equation: $y = x^2 + 4x + 2$

perfect square equation: $y = x^2 + 4x + 4$

We have to adjust \uparrow to get back to original.

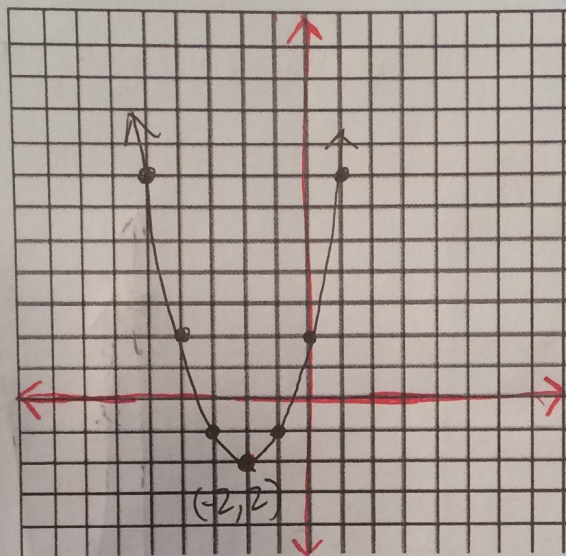
adjusted: $y = (x^2 + 4x + 4) - 2$

vertex form: $y = (x+2)^2 - 2$

- b. Is the equation you have written equivalent to the original equation? If not, what adjustments need to be made? Why?

Yes, once we subtract two off of the perfect square equation it would be equal.

- c. Identify the vertex and graph the parabola with three accurate points on both sides of the line of symmetry.



$$y = (x+2)^2 - 2$$

\swarrow shift left 2 \searrow shift down 2

Vertex: $(-2, -2)$

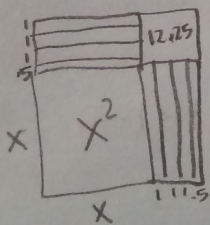
not stretched so follow
 over 1, up 1
 over 2, up 4
 over 3, up 9

5. Jenny hoped that she wasn't going to need to figure out how to complete the square on an equation where b is an odd number. Of course, that was the next problem. Help Jenny to find the vertex of the parabola for this quadratic function:

$$g(x) = x^2 + 7x + 10$$

$$\downarrow$$

$$\frac{7}{2} = 3.5$$



perfect square equation: $x^2 + 7x + 12.25$

We need to subtract 2.25 to get back to 10 in the original equation.
 adjusted: $x^2 + 7x + 12.25 - 2.25$

Vertex Form: $g(x) = (x+3.5)^2 - 2.25$

Vertex: $(-3.5, -2.25)$

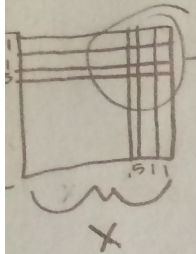
6. Don't worry if you had to think hard about #5. Jenny has to do a couple more:

a. $g(x) = x^2 - 5x + 3$

b. $g(x) = x^2 - x - 5$

\downarrow
 $-\frac{5}{2} = -2.5$

\downarrow
 $-\frac{1}{2} = -0.5 \rightarrow (-0.5)^2 = 0.25$



$g(x) = x^2 - 5x + 6.25 - 3.25$

$g(x) = (x - 2.5)^2 - 3.25$

$g(x) = (x^2 - x + 0.25) - 5.25$

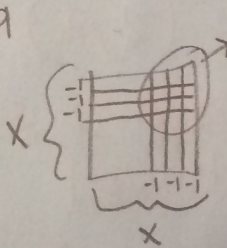
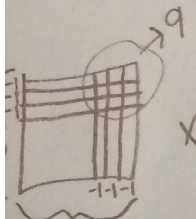
$g(x) = (x - 0.5)^2 - 5.25$

side length: $x - 2.5$

vertex: $(2.5, -3.25)$

vertex: $(0.5, -5.25)$

7. It just gets better! Help Jenny find the vertex and graph the parabola for the quadratic function: $h(x) = 2x^2 - 12x + 17$



9 2 squares

perfect: $2x^2 - 12x + 18$
 or

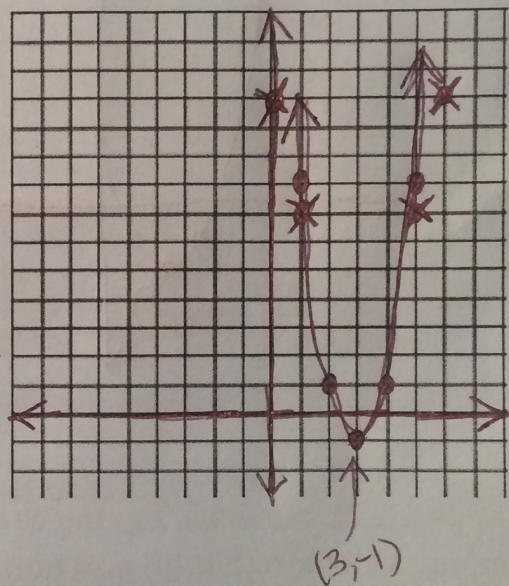
$2(x^2 - 6x + 9)$

We have to -1 to adjust the perfect square equation

$h(x) = 2x^2 - 12x + 18 - 1$

$h(x) = 2(x - 3)^2 - 1$

vertex: $(3, -1)$



From vertex:
 over 1, up 2
 over 2, up 8

8. This one is just too cute—you've got to try it! Find the vertex and describe the parabola that is the graph of: $f(x) = \frac{1}{2}x^2 + 2x - 3$

$\frac{1}{2}(x^2 + 4x - 6)$ perfect: $\frac{1}{2}(x^2 + 4x + 4)$

$\frac{1}{2} \cdot 4 = 2 \rightarrow 2^2 = 4$

We have to -5 to get back to the original

$f(x) = \frac{1}{2}(x^2 + 4x + 4) - 5$

$f(x) = \frac{1}{2}(x + 2)^2 - 5$